

# Measurement of the $t$ distribution in diffractive photoproduction at HERA

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**Abstract.** Photon diffractive dissociation,  $\gamma p \rightarrow Xp$ , has been studied at HERA with the ZEUS detector using  $ep$  interactions where the virtuality  $Q^2$  of the exchanged photon is smaller than  $0.02 \text{ GeV}^2$ . The squared four-momentum  $t$  exchanged at the proton vertex was determined in the range  $0.073 < |t| < 0.40 \text{ GeV}^2$  by measuring the scattered proton in the ZEUS Leading Proton Spectrometer. In the photon-proton centre-of-mass energy interval  $176 < W < 225 \text{ GeV}$  and for masses of the dissociated photon system  $4 < M_X < 32 \text{ GeV}$ , the  $t$  distribution has an exponential shape,  $dN/d|t| \propto \exp(-b|t|)$ , with a slope parameter  $b = 6.8 \pm 0.9$  (stat.)  $^{+1.2}_{-1.1}$  (syst.)  $\text{GeV}^{-2}$ .

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## 1 Introduction

The reaction  $\gamma p \rightarrow Xp$ , in which the photon diffractively dissociates into an hadronic state  $X$  with mass  $M_X$ , has been investigated with real photons at a photon-proton centre-of-mass energy  $W$  of about 14 GeV [1]. Recently it has also been studied at HERA using the process  $ep \rightarrow eXp$  for photon virtualities  $Q^2 < 0.02$  GeV<sup>2</sup> and  $W \approx 200$  GeV [2,3]. The comparison of the fixed target data and the HERA data indicates that the dissociation of real photons has similar characteristics to the dissociation of hadrons, as expected in the framework of Vector Meson Dominance (VMD) [4,5]. In this model, the photon is assumed to fluctuate into a virtual vector meson prior to the interaction with the proton. The interaction can be described by Regge phenomenology [6] and, at high energy, is dominated by the exchange of an object with the quantum numbers of the vacuum, referred to as the pomeron. An exponential fall of the differential cross section  $d\sigma/d|t| \propto \exp(-b|t|)$ , at small values of  $|t|$ , is a typical feature of diffraction; here  $t$  is the square of the four-momentum transfer at the proton vertex. Regge theory also predicts that the diffractive peak shrinks as  $W$  increases according to  $b = b_0 + 2\alpha' \ln(W^2/M_X^2)$ , where  $b_0$  and  $\alpha'$  are constants [6,7].

The studies of diffractive real photon dissociation at HERA have so far focussed on the shape of the  $M_X$  spectrum [2,3]. The  $t$  distribution for the reaction  $\gamma p \rightarrow Xp$  has been measured only by the fixed target experiment [1],

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which found that in the range  $1.4 < M_X < 3$  GeV and for  $0.02 < |t| < 0.1$  GeV<sup>2</sup> the  $t$  dependence is exponential with a  $t$ -slope  $b \approx 5$  GeV<sup>-2</sup>. At HERA, measurements of the  $t$  distribution have been performed for the diffractive dissociation of virtual photons in the range  $5 < Q^2 < 20$  GeV<sup>2</sup> [8], and for elastic vector meson production,  $\gamma p \rightarrow Vp$ , both with real and with virtual photons [9–18]. In all cases the distribution has an approximately exponential shape. The  $t$ -slope is  $b = 7.2 \pm 1.1$  (stat.)  $_{-0.9}^{+0.7}$  (syst.) GeV<sup>-2</sup> for the diffractive dissociation of virtual photons at  $\langle Q^2 \rangle = 8$  GeV<sup>2</sup>. For elastic  $\rho^0$  production  $b$  depends only weakly on  $W$  but varies from approximately 10 GeV<sup>-2</sup> for  $Q^2 \approx 0$  [9–11] to approximately 5–7 GeV<sup>-2</sup> for  $\langle Q^2 \rangle = 10$  GeV<sup>2</sup> [12,13]. It is therefore interesting to extend these measurements to diffractive real photon dissociation.

In this paper we report the first determination at HERA of the  $t$  distribution for the process  $\gamma p \rightarrow Xp$ , where  $\gamma$  is a photon with  $Q^2 < 0.02$  GeV<sup>2</sup>. The present measurement is based on a sample of photoproduction events collected using the reaction  $ep \rightarrow eXp$  at  $W \approx 200$  GeV [3]. The sample was defined by the requirement that the scattered positron be measured in a calorimeter close to the outgoing positron beam line and a final state proton carrying at least 97% of the incoming proton momentum be detected in the ZEUS Leading Proton Spectrometer (LPS) [11]. The LPS was also used to measure the transverse momentum of the proton, from which  $t$  was calculated. This is a technique similar to that used to measure the  $t$  distribution in the photoproduction of  $\rho^0$  mesons,  $\gamma p \rightarrow \rho^0 p$  [11], and for the diffractive dissociation of virtual photons,  $\gamma^* p \rightarrow Xp$  [8].

## 2 Experimental set-up

### 2.1 HERA

The data presented here were collected in 1994 at HERA which operated with 820 GeV protons and 27.5 GeV positrons. The proton and positron beams each contained 153 colliding bunches, together with 17 additional unpaired proton and 15 unpaired positron bunches. These additional bunches were used for background studies. The integrated luminosity for the present study, which required the LPS to be in operation, is  $0.9 \text{ pb}^{-1}$ .

### 2.2 The ZEUS detector

A detailed description of the ZEUS detector can be found elsewhere [19,20]. A brief outline of the components which are most relevant for this analysis is given below. Throughout this paper the standard ZEUS coordinate system is used, which has the origin at the nominal interaction point, the  $Z$  axis pointing in the proton beam direction, hereafter referred to as “forward”, the  $X$  axis pointing horizontally towards the centre of HERA and the  $Y$  axis pointing upwards. The polar angle  $\theta$  is defined with respect to the  $Z$  direction.

Charged particles are measured by the inner tracking detectors which operate in a magnetic field of 1.43 T provided by a thin superconducting solenoid. Immediately surrounding the beam-pipe is the vertex detector (VXD), a drift chamber which consists of 120 radial cells, each with 12 sense wires [21]. It is surrounded in turn by the central tracking detector (CTD), which consists of 72 cylindrical drift chamber layers, organized into 9 superlayers covering the polar angle region  $15^\circ < \theta < 164^\circ$  [22].

For the energy measurement the high resolution depleted-uranium scintillator calorimeter (CAL) is used [23]. It is divided into three parts, forward (FCAL) covering the pseudorapidity<sup>1</sup> region  $4.3 > \eta > 1.1$ , barrel (BCAL) covering the central region  $1.1 > \eta > -0.75$  and rear (RCAL) covering the backward region  $-0.75 > \eta > -3.8$ . Holes of  $20 \times 20 \text{ cm}^2$  in the centre of FCAL and RCAL accommodate the HERA beam-pipe. Each of the calorimeter parts is subdivided into towers, which in turn are segmented longitudinally into electromagnetic (EMC) and hadronic (HAC) sections. These sections are further subdivided into cells, which are read out by two photomultiplier tubes. Under test beam conditions, the energy resolution of the calorimeter was measured to be  $\sigma_E/E = 0.18/\sqrt{E(\text{GeV})}$  for electrons and  $\sigma_E/E = 0.35/\sqrt{E(\text{GeV})}$  for hadrons. The calorimeter noise, dominated by the uranium radioactivity, is in the range 15–19 MeV for an EMC cell and 24–30 MeV for a HAC cell.

The luminosity is determined from the rate of the Bethe-Heitler process,  $ep \rightarrow e\gamma p$ , where the photon is measured with a lead-scintillator sandwich calorimeter (LUMI- $\gamma$ ) located at  $Z = -107 \text{ m}$  in the HERA tunnel downstream of the interaction point in the direction of the outgoing positrons [24]. A similar calorimeter (LUMI- $e$ ) at  $Z = -35 \text{ m}$  detects positrons scattered at very small angles. In this analysis, the LUMI- $e$  was used to tag photoproduction events with positrons scattered at angles up to about 5 mrad and to measure the scattered positron energy,  $E'_e$ . The LUMI- $e$  covers the range  $7 < E'_e < 21 \text{ GeV}$ . The energy resolution of both calorimeters is  $\sigma_E/E = 0.18/\sqrt{E(\text{GeV})}$ .

The Leading Proton Spectrometer (LPS) [11] detects charged particles scattered at small angles and carrying a substantial fraction,  $x_L$ , of the incoming proton momentum; these particles remain in the beam-pipe and their trajectory is measured by a system of silicon micro-strip detectors very close (typically a few mm) to the proton beam. The detectors are grouped in six stations, S1 to S6, placed along the beam line in the direction of the outgoing protons, at 23.8 m, 40.3 m, 44.5 m, 63.0 m, 81.2 m and 90.0 m from the interaction point. The track deflections induced by the magnets in the proton beam line allow a momentum analysis of the scattered proton. For the present measurements, only the stations S4, S5 and S6 were used. With this configuration, for  $x_L$  close to unity, resolutions of 0.4% on the longitudinal momentum and 5 MeV on the transverse momentum have been achieved. The effective transverse momentum resolution

is, however, dominated by the intrinsic transverse momentum spread of the proton beam at the interaction point which is  $\approx 40 \text{ MeV}$  in the horizontal plane and  $\approx 90 \text{ MeV}$  in the vertical plane. For  $x_L$  close to unity, the LPS covers the range  $0.25 \lesssim p_T \lesssim 0.65 \text{ GeV}$ , where  $p_T$  is the transverse momentum of the proton with respect to the incoming beam direction. As discussed previously [11], the incoming beam direction and the beam position with respect to each station are determined using the reaction  $ep \rightarrow e\rho^0 p$  at  $Q^2 \approx 0$ . Protons with  $p_T < 0.2 \text{ GeV}$  and  $x_L \approx 1$  are too close to the beam to be measured. For the events considered here the geometric acceptance of the LPS is approximately 6%.

## 3 Data selection and background subtraction

### 3.1 Trigger

ZEUS uses a three-level trigger system [19,20]. At the first-level a coincidence between signals in the LUMI- $e$  and in the RCAL was required. An energy deposit greater than 5 GeV was required in the LUMI- $e$ . In the RCAL the deposit had to be larger than 464 MeV (excluding the towers immediately adjacent to the beam-pipe) or 1250 MeV (including those towers). The angular acceptance of the LUMI- $e$  limits the  $Q^2$  range to the region  $Q^2 < 0.02 \text{ GeV}^2$ . The small RCAL threshold essentially selects all photoproduction events. The second and third trigger levels were mainly used to reject beam related background. Parts of the data stream were prescaled [3,25] in order to reduce the high event rate resulting from the large photoproduction cross section.

### 3.2 Reconstruction of variables

The photon-proton centre-of-mass energy squared,  $W^2 = (q+p)^2$ , where  $q$  and  $p$  are the virtual photon and the proton four-momenta, respectively, was determined by  $W^2 \approx ys$ , with  $y \approx E_\gamma/E_e = (E_e - E'_e)/E_e$  and  $s$  the squared centre-of-mass energy of the positron-proton system; here  $E_\gamma$  is the energy of the exchanged photon and  $E_e$  denotes the energy of the incoming positron. The  $W$  resolution is 7 GeV at  $W = 176 \text{ GeV}$  and improves to 4.5 GeV at  $W = 225 \text{ GeV}$ .

The mass  $M_X$  of the dissociated photon system was reconstructed [3] by combining the information from the LUMI- $e$  and the CAL:

$$\begin{aligned} M_X &= \sqrt{E^2 - P^2} \approx \sqrt{(E - P_Z) \cdot (E + P_Z)} \\ &= \sqrt{2E_\gamma \cdot (E + P_Z)}, \end{aligned} \quad (1)$$

where  $E$  is the energy of the hadronic system observed in the CAL; the total momentum of the hadronic system,  $P$ , approximately equals the longitudinal component,  $P_Z$ , as the transverse component generally is small in the case of photoproduction events. The following formula was used

<sup>1</sup> The pseudorapidity  $\eta$  is defined as  $\eta = -\ln(\tan(\theta/2))$

for the mass reconstruction:

$$M_{X \text{ rec}} = a_1 \cdot \sqrt{2E_\gamma \cdot \left( \sum_{\text{cond}} E_i + \sum_{\text{cond}} E_i \cos \theta_i \right)} + a_2. \quad (2)$$

The quantities  $E_i$  and  $\theta_i$  denote the energy and the polar angle of CAL condensates, defined as groups of adjacent cells with total energy of at least 100 MeV, if all the cells belong to the EMC, or 200 MeV otherwise. These cuts reduce the effect of noise on the mass reconstruction. They were applied in addition to a noise suppression algorithm which discarded all EMC (HAC) cells with energy below 60 MeV (110 MeV); for isolated cells the thresholds were increased to 80 MeV (120 MeV). The coefficients  $a_1$  and  $a_2$  correct for the effects of energy loss in the inactive material in front of the CAL and of energy deposits below the threshold. Their values,  $a_1 = 1.14$  and  $a_2 = 1.2$  GeV, were taken from [3]. The masses in the range  $4 < M_X < 40$  GeV are reconstructed with a resolution  $\sigma_{M_X}/M_X \approx 0.8/\sqrt{M_X}(\text{GeV})$  and an offset smaller than 0.5 GeV [3].

The variable  $t = (p-p')^2$ , where  $p$  and  $p'$  are the incoming and the scattered proton four-momenta, respectively, can be evaluated as  $t \approx -(p_T^2/x_L)[1 + (M_p^2/p_T^2)(1-x_L)^2]$ . Both  $p_T$  and  $x_L$  were measured with the LPS. For the data considered here, which have  $x_L$  close to unity, the approximation  $t \approx -p_T^2/x_L$  was used. Since, as mentioned earlier, the incoming proton beam has an intrinsic transverse momentum spread of  $\sigma_{p_x} \approx 40$  MeV and  $\sigma_{p_y} \approx 90$  MeV, which is much larger than the LPS resolution in transverse momentum, the measured value of  $t$  is given by the convolution of the true  $t$  distribution and the effect of the beam spread. Because of this we make a distinction between the true value of  $t$  and the measured value,  $t_{\text{apparent}} = -p_T^2/x_L$ .

### 3.3 Offline selection

To select the final sample, the following conditions were imposed on the reconstructed data:

- A scattered positron in the LUMI- $e$  with energy in the range  $12 < E'_e < 18$  GeV, corresponding to  $176 < W < 225$  GeV.
- An interaction vertex reconstructed by the tracking detectors.
- Mass of the dissociated photon system in the range  $4 < M_{X \text{ rec}} < 32$  GeV. The lower limit eliminates the region dominated by resonance production; it also reflects the lower limit of  $M_X = 1.7$  GeV for which Monte Carlo events were generated (cf. Section 4). The upper limit is a consequence of the limit on  $x_L$  (see below), since  $M_X^2 \approx W^2(1-x_L)$ .

In addition, the detection of a high momentum proton in the LPS was required [11]:

- One track in the LPS with  $x_L > 0.97$  was required. This is used to select diffractive events in which the proton remains intact.

- Protons with reconstructed trajectories closer than 0.5 mm to the wall of the beam-pipe, at any point between the vertex and the last station hit, were rejected. This eliminates any sensitivity of the acceptance to possible misalignments of the HERA beam-pipe elements. In addition badly reconstructed tracks are removed.
- The  $p_T$  range was restricted to the interval  $0.27 < p_T < 0.63$  GeV, thereby removing regions where the acceptance of the LPS is very small or changes rapidly [11].

After these selections, 641 events remained.

### 3.4 Background

The background contamination in the sample was mainly due to two sources.

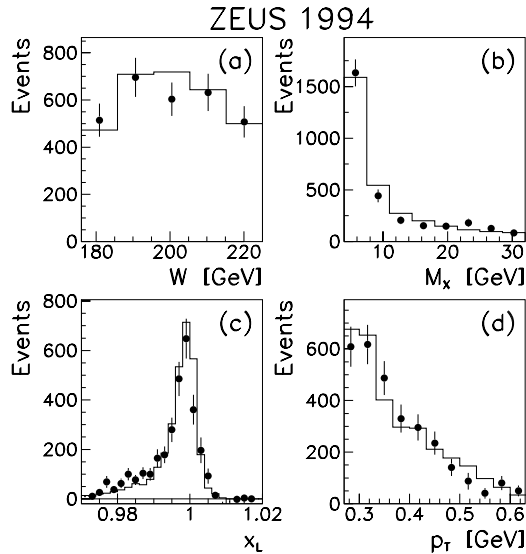
1. Some activity in the RCAL can accidentally overlap with the scattered positron of a bremsstrahlung event ( $ep \rightarrow e\gamma p$ ) in the LUMI- $e$  [3]. A large fraction of this background can be identified since the bremsstrahlung photon is accepted by the LUMI- $\gamma$ . For bremsstrahlung, one has  $E'_e + E_\gamma = E_e$ , where  $E_\gamma$  is the energy of the radiated photon. For such events the energy deposits in the LUMI- $e$  and the LUMI- $\gamma$  calorimeters thus sum up to the positron beam energy. These events were removed.

The unidentified events were statistically subtracted by including the identified background events with negative weights in all the distributions, thereby compensating for the unidentified background events [26,27]. This subtraction was less than 3%.

2. A proton beam-halo track in the LPS can accidentally overlap with an event satisfying the trigger and the selection cuts applied to the variables measured with the central ZEUS detector (beam-halo event). The term beam-halo track refers to a proton with energy close to that of the beam originating from an interaction of a beam proton with the residual gas in the pipe or with the beam collimator jaws. Obviously, a beam-halo track is uncorrelated with the activity in the central ZEUS detector. For such a beam-halo event, energy and momentum conservation are not necessarily satisfied; in particular the quantity  $(E + P_Z + 2P_Z^{LPS})$ , where  $P_Z^{LPS}$  is the  $Z$  component of the proton momentum measured in the LPS, may exceed the kinematic limit of 1640 GeV. The condition  $(E + P_Z + 2P_Z^{LPS}) > 1655$  GeV (thereby including the effects of resolution) identifies such events, which thus were rejected.

In order to evaluate the residual contamination after all cuts, the distribution of  $2P_Z^{LPS}$  for identified beam-halo events was randomly mixed with the  $(E + P_Z)$  distribution for all events, so as to create a distribution of  $(E + P_Z + 2P_Z^{LPS})$  for halo events. The observed  $(E + P_Z + 2P_Z^{LPS})$  distribution was then fitted as the sum of the diffractive Monte Carlo contribution (cf. Sect. 4) and the beam-halo contribution just discussed. The relative normalisation of the two terms was left as a





**Fig. 1.** Distributions as a function of **a**  $W$ , **b**  $M_X$ , **c**  $x_L$  and **d**  $p_T$  for the data (points) and the Monte Carlo events (histogram). The error bars indicate the statistical uncertainty of the data. The number of data events is corrected for the trigger prescale factors and the background

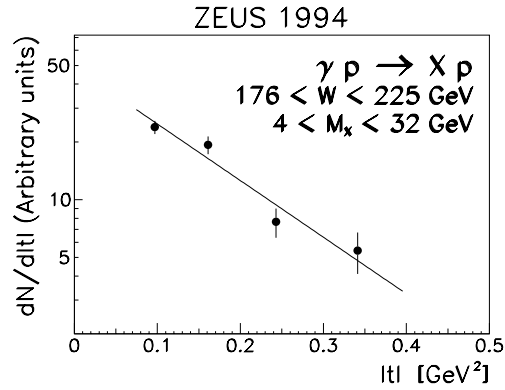
free parameter. For events with  $(E + P_Z + 2P_Z^{LPS}) < 1655$  GeV, the fraction of beam-halo events thus was estimated to be  $(6.3 \pm 1.2)\%$ . Here again the identified background events were included with negative weights in all the distributions in order to compensate for the unidentified beam-halo events.

The number of events remaining after the background subtraction, i.e. after removing the identified bremsstrahlung and beam-halo events and after including the effect of the negative weights, was 515. The contribution from non-single diffractive dissociation processes, e.g. double diffractive dissociation, is expected to be of the order of a few per cent [8] and was not subtracted.

Figure 1 shows the observed  $W$ ,  $M_X$ ,  $x_L$  and  $p_T$  distributions for the selected events after background subtraction and including the correction for the effects of the trigger prescale factors.

## 4 Monte Carlo simulation and acceptance determination

The reaction  $ep \rightarrow eXp$  was simulated using a Monte Carlo generator [28] based on a model calculation by Nikolaev and Zakharov [29]. The generated  $M_X$  distribution was reweighted with the sum of a pomeron-pomeron-pomeron [7] ( $d\sigma/dM_X^2 \propto 1/M_X^2$ ) and a pomeron-pomeron-reggeon [7] contribution ( $d\sigma/dM_X^2 \propto 1/M_X^3$ ), so as to obtain a satisfactory agreement between data and Monte Carlo. As discussed in Sect. 5, however, the present results on the  $t$  distribution are largely independent of the details of the  $M_X$  spectrum simulation in the mass range considered in the analysis.



**Fig. 2.** Differential distribution  $dN/d|t|$  for photon diffractive dissociation,  $\gamma p \rightarrow Xp$ , in the kinematic region  $176 < W < 225$  GeV and  $4 < M_X < 32$  GeV. The vertical bars indicate the size of the statistical uncertainties. The line is the result of the fit described in the text. The scale on the vertical axis is arbitrary

All generated events were passed through the standard ZEUS detector simulation, based on the GEANT program [30], and through the trigger simulation package. The simulation also includes the geometry of the beam-pipe apertures, the HERA magnets and their fields. The spread of the interaction vertex position was also simulated and so were the proton beam angle with respect to the nominal direction and its dispersion at the interaction point. The simulated events were then passed through the same reconstruction and analysis programs as the data. In Fig. 1 the distributions for the reconstructed Monte Carlo events as a function of  $W$ ,  $M_X$ ,  $x_L$  and  $p_T$  are compared with those of the data. The distributions of the simulated events were normalised to the observed number of events, corrected for the effects of the prescale and of the background subtraction. The agreement between the data and the Monte Carlo distributions is satisfactory.

The acceptance was computed as the ratio of the number of reconstructed Monte Carlo events in a bin of a given variable and the number of generated events in that bin. The acceptance thus includes the effects of the geometric acceptance of the apparatus, its efficiency and resolution, as well as the trigger and reconstruction efficiencies.

## 5 Results and discussion

The acceptance corrected  $t$  distribution,  $dN/d|t|$ , is shown in Fig. 2. It was obtained by correcting the measured  $t_{apparent}$  distribution bin by bin with the acceptance determined from the Monte Carlo simulation described above.

The data were fitted with the function:

$$\frac{dN}{d|t|} = A \cdot e^{-b|t|}, \quad (3)$$

where  $A$  is a constant. The resulting value of the  $t$ -slope is

$$b = 6.8 \pm 0.9 \text{ (stat.)}_{-1.1}^{+1.2} \text{ (syst.) GeV}^{-2},$$

**Table 1.** A compilation of results for the  $t$ -slope for the reaction  $\gamma p \rightarrow Xp$ . The present result is listed together with those from [1] for real photons and that of [8] for virtual photons

	Present result	Ref. [1]	Ref. [8]
$\langle Q^2 \rangle / \text{GeV}^2$	$\approx 0$	0	8
$W$ range/GeV	176–225	12–17	50–270
$M_X$ range/GeV	4–32	1.4–1.7, 1.7–2.2, 2.2–3	2–27
$ t $ range/GeV <sup>2</sup>	0.073–0.4	0.02–0.1	0.073–0.4
$b/\text{GeV}^{-2}$	$6.8 \pm 0.9$ (stat.) $^{+1.2}_{-1.1}$ (syst.)	$4.2 \pm 1.4, 6.3 \pm 1.3, 5.1 \pm 1.3$	$7.2 \pm 1.1$ (stat.) $^{+0.7}_{-0.9}$ (syst.)

in the kinematic region  $4 < M_X < 32$  GeV,  $0.073 < |t| < 0.40$  GeV<sup>2</sup> and  $176 < W < 225$  GeV. In this region, the average value of  $W$  is 200 GeV and the average value of  $M_X$  is 11 GeV. The result of the fit is indicated by the continuous line on Fig. 2.

The analysis was repeated for the two  $M_X$  ranges  $4 < M_X < 8$  GeV and  $8 < M_X < 32$  GeV. The results,  $b = 7.0 \pm 1.3$  GeV<sup>-2</sup> and  $b = 6.5 \pm 1.3$  GeV<sup>-2</sup>, indicate no variation with  $M_X$  within the present sensitivity.

The quoted systematic uncertainty on  $b$  ( $\Delta b$ ) was obtained by modifying the requirements and the analysis procedures as listed below:

- Sensitivity to the selection of the proton track (cf. [11]):
  - The sensitivity to the proton beam tilt with respect to the nominal was evaluated by systematically shifting  $p_T$  by 10 MeV.
  - The track selection requirements were tightened.
  - Events with  $p_X^{LPS} > 0$  and with  $p_X^{LPS} < 0$  were analysed separately, as a check of possible relative rotations of the LPS detector stations.
  - The data were divided into a “low acceptance” and a “large acceptance” sample depending on the position of the LPS stations. The latter varied slightly from run to run.

The last three contributions dominate; by summing all four in quadrature,  $\Delta b = \pm 1.0$  GeV<sup>-2</sup> was obtained.

- Sensitivity to the other selection cuts and acceptance corrections:
  - The  $W$  range was restricted to  $195 < W < 215$  GeV, leading to  $b = 6.7 \pm 1.4$  GeV<sup>-2</sup>.
  - The  $M_X$  distribution in the Monte Carlo was varied between  $d\sigma/dM_X^2 \propto (1/M_X)^{1.5}$  and  $d\sigma/dM_X^2 \propto (1/M_X)^3$ . The corresponding variation of  $b$  was at most  $\pm 0.2$  GeV<sup>-2</sup>.
  - The vertex requirement was removed or restricted to  $|Z_{vertex}| < 50$  cm. The effect on  $b$  was at most  $\pm 0.4$  GeV<sup>-2</sup>.

Summing these contributions to  $\Delta b$  in quadrature yields  $\Delta b = \pm 0.5$  GeV<sup>-2</sup>.

- Background corrections: the size of the beam-halo background was varied by two standard deviations, yielding negligible effects. The bremsstrahlung background correction was removed altogether, causing changes in the result smaller than 0.1 GeV<sup>-2</sup>.
- Evaluation of the  $t$ -slope:
  - The  $t$ -slope was determined with an alternative method discussed in detail in [11,31]. One can ex-

press the  $t_{apparent}$  distribution as a convolution of (3) and a two-dimensional Gaussian distribution representing the beam transverse momentum distribution. The slope parameter  $b$  can then be determined by fitting the convolution of (3) and the two-dimensional Gaussian to the acceptance corrected  $t_{apparent}$  distribution. This method has the advantage that the data can be binned in  $t_{apparent}$  for which the resolution is much better than for  $t$ , as discussed earlier. The value of  $b$  thus obtained was  $b = 7.3 \pm 0.9$  GeV<sup>-2</sup>.

- The  $t$ -slope was also obtained with a third method: the  $t_{apparent}$  distributions in the data and in the Monte Carlo were compared and the Monte Carlo  $t$  distribution at the generator level was reweighted until the  $\chi^2$  of the comparison between data and Monte Carlo reached a minimum. The result thus found differed from the nominal one by less than 0.1 GeV<sup>-2</sup>.
- The sensitivity to the binning in  $t$  was studied by using an unbinned maximum likelihood method for the fit, which gave a result differing from the nominal one by less than 0.1 GeV<sup>2</sup>.

The quadratic sum of these effects contributes  $\Delta b = ^{+0.5}_{-0.1}$  GeV<sup>-2</sup>.

All contributions were summed in quadrature, yielding a total systematic error  $\Delta b = ^{+1.2}_{-1.1}$  GeV<sup>-2</sup>.

Table 1 lists the present result together with those of the Fermilab photoproduction experiment E612 [1] and that obtained by ZEUS for  $\langle Q^2 \rangle = 8$  GeV<sup>2</sup> [8]. The present result agrees within errors with both. This agreement suggests that at fixed  $W$  there is little dependence of the slope on  $Q^2$  and that for real photons the  $W$  dependence is not strong. Note that the  $t$  range of our measurement is different from that of [1], which is  $0.02 < |t| < 0.1$  GeV<sup>2</sup>. A direct comparison should therefore be made with caution: for example, in elastic  $\pi p$  scattering [32], the  $t$ -slope measured in the range  $0.1 \lesssim |t| \lesssim 0.4$  GeV<sup>2</sup> is about 1.2 GeV<sup>-2</sup> lower than in the range covered by [1]; this difference is of the same size as the errors of our measurement.

The weak  $Q^2$  dependence of the  $t$ -slope in diffractive photon dissociation may be contrasted with the change with  $Q^2$  observed for elastic  $\rho^0$  meson production [9–13], where  $b$  decreases by approximately 3–5 GeV<sup>-2</sup> when going from  $Q^2 \approx 0$  to  $Q^2 \approx 10$  GeV<sup>2</sup>. If factorisation of

the diffractive vertices [32] is assumed, the amplitudes for the reactions  $\gamma p \rightarrow Xp$  and  $\gamma p \rightarrow \rho^0 p$  are proportional to the products of vertex functions  $G_{\gamma X}(Q^2, t) \cdot G_{pp}(t)$  and  $G_{\gamma\rho^0}(Q^2, t) \cdot G_{pp}(t)$ , respectively. In this framework, the  $t$ -slope includes the sum of the contributions from the  $\gamma$ - $X$  or  $\gamma$ - $\rho^0$  vertex and from the  $p$ - $p$  vertex. The comparison of the  $\gamma p \rightarrow Xp$  and  $\gamma p \rightarrow \rho^0 p$  slopes indicates that the vertex function  $G_{\gamma X}(Q^2, t)$  has a weaker dependence on  $Q^2$  than  $G_{\gamma\rho^0}(Q^2, t)$ . A rapid  $Q^2$  dependence of  $G_{\gamma\rho^0}(Q^2, t)$  is expected in pQCD inspired models of elastic vector meson production [33], reflecting the decrease with  $Q^2$  of the transverse size of the quark-antiquark pair into which the photon fluctuates before interacting with the proton. A weak  $Q^2$  dependence of the function  $G_{\gamma X}(Q^2, t)$  is also expected in the framework of various models of diffractive dissociation of photons [34].

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